



Multiplicative Method

Cipher based on multiply each character by Key, where k and 26 are relatively; so that the letters of the alphabet produce a complete set of residues, so that case the key must be an odd number and not equal to 13.

K_1	1	3	5	7	9	11	15	17	19	21	23	25
K_1^{-1}	1	9	21	15	3	19	7	23	11	5	17	25

Note: *Keep in your mine that*

k: the key is used for the encryption process

k^{-1} : the key is used for decryption process

Encryption process

A system of encryption in which each letter of message is replaced with another characters, to produce the cipher text according to this formula below:

$$C = (P * k) \bmod 26$$

Decryption process

A system of decryption in which each letter of ciphertext is replaced with another characters to produce the plaintext or the message according to this formula below:

$$P = (C * k^{-1}) \bmod 26$$

**Example1**

Use the multiplicative method to encrypt and decrypt the message "Computer" if the key is 5.

Solution**Encryption process:**

By applying the encryption process formula: $C = (P * k) \bmod 26$ on the plaintext

$$\begin{array}{l}
 E(c) = 2 * 5 \bmod 26 \Rightarrow 10 \bmod 26 \Rightarrow k \\
 E(o) = 14 * 5 \bmod 26 \Rightarrow 70 \bmod 26 \Rightarrow 18 \Rightarrow s \\
 E(m) = 12 * 5 \bmod 26 \Rightarrow 60 \bmod 26 \Rightarrow 8 \Rightarrow i \\
 E(p) = 15 * 5 \bmod 26 \Rightarrow 75 \bmod 26 \Rightarrow 23 \Rightarrow x \\
 E(u) = 20 * 5 \bmod 26 \Rightarrow 100 \bmod 26 \Rightarrow 22 \Rightarrow w \\
 E(t) = 19 * 5 \bmod 26 \Rightarrow 95 \bmod 26 \Rightarrow 17 \Rightarrow r \\
 E(e) = 4 * 5 \bmod 26 \Rightarrow 20 \bmod 26 \Rightarrow 20 \Rightarrow u \\
 E(r) = 17 * 5 \bmod 26 \Rightarrow 85 \bmod 26 \Rightarrow 7 \Rightarrow h
 \end{array}$$

The ciphertext is "ksixwruh"



Decryption process:

By applying the Decryption process formula $P = (C * k^{-1}) \bmod 26$ on the ciphertext "ksixwruh" to produce the original message

$$\begin{aligned}
 D(k) &= 10 * 21 \bmod 26 \Rightarrow 210 \bmod 26 = 2 \Rightarrow c \\
 D(s) &= 18 * 21 \bmod 26 \Rightarrow 378 \bmod 26 = 14 \Rightarrow o \\
 D(i) &= 8 * 21 \bmod 26 \Rightarrow 168 \bmod 26 = 12 \Rightarrow m \\
 D(x) &= 23 * 21 \bmod 26 \Rightarrow 483 \bmod 26 = 15 \Rightarrow p \\
 D(w) &= 22 * 21 \bmod 26 \Rightarrow 462 \bmod 26 = 20 \Rightarrow u \\
 D(r) &= 17 * 21 \bmod 26 \Rightarrow 357 \bmod 26 = 19 \Rightarrow t \\
 D(u) &= 20 * 21 \bmod 26 \Rightarrow 420 \bmod 26 = 4 \Rightarrow e \\
 D(h) &= 7 * 21 \bmod 26 \Rightarrow 147 \bmod 26 = 17 \Rightarrow r
 \end{aligned}$$

The plaintext is "computer"